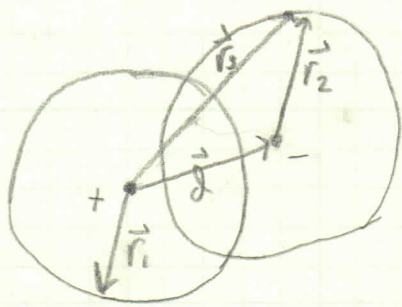


2.18



$$\vec{r}_3 = \vec{d} + \vec{r}_2$$

$$\hat{r}_3 = \frac{\vec{d} + \vec{r}_2}{|\vec{d} + \vec{r}_2|} = \frac{\vec{d} + |\vec{r}_2| \hat{r}_2}{|\vec{d} + \vec{r}_2|}$$

$$\hat{r}_2 = \frac{\vec{r}_2}{|\vec{r}_2|}$$

$$\Rightarrow \frac{|\vec{d} + \vec{r}_2| \hat{r}_3 - \vec{d}}{|\vec{r}_2|} = \hat{r}_2$$

$$\text{for just } \vec{r}_1, \quad \vec{E}_1 = \frac{|\vec{r}_1| \rho}{3\epsilon_0} \hat{r}_3$$

$$\text{for } \vec{r}_2, \quad \vec{E}_2 = \frac{|\vec{r}_3 - \vec{d}| \rho}{3\epsilon_0} \hat{r}_2$$

$$\hat{r}_2 = \frac{|\vec{r}_3| \hat{r}_3 - \vec{d}}{|\vec{r}_2|}$$

then for the region of overlap, w/  $\vec{r}_1 = \vec{r}_3$ .

$$\vec{E}_{\text{overlap}} = \vec{E}_1 + \vec{E}_2 = \frac{|\vec{r}_3| \rho}{3\epsilon_0} \hat{r}_3 - \frac{|\vec{r}_2| \rho}{3\epsilon_0} \hat{r}_2$$

$$= \frac{|\vec{r}_3| \rho}{3\epsilon_0} \hat{r}_3 - \frac{\rho}{3\epsilon_0} |\vec{r}_2| \frac{|\vec{r}_3| \hat{r}_3 - \vec{d}}{|\vec{r}_2|} = \frac{\rho}{3\epsilon_0} \vec{d}$$